

# Towards a Hierarchical Approach for Outlier Detection in Industrial Production Settings

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## ABSTRACT

In the context of Industry 4.0, the degree of cross-linking between machines, sensors, and production lines increases rapidly. However, this trend also offers the potential for the improvement of outlier scores, especially by combining outlier detection information between different production levels. The latter, in turn, offer various other useful aspects like different time series resolutions or context variables. When utilizing these aspects, valuable outlier information can be extracted, which can be then used for condition-based monitoring, alert management, or predictive maintenance. In this work, we compare different types of outlier detection methods and scores in the light of the aforementioned production levels with the goal to develop a model for outlier detection that incorporates these production levels. The proposed model, in turn, is basically inspired by a use case from the field of additive manufacturing, which is also known as industrial 3D-printing. Altogether, our model shall improve the detection of outliers by the use of a hierarchical structure that utilizes production levels in industrial scenarios.

## KEYWORDS

Outlier Detection, Production Level, Outlierness

## 1 INTRODUCTION

In general, outlier detection can be used in the context of production control to provide *Condition Monitoring*, generate *Alerts*, discover *Concept Shifts*, or serve as an indicator for *Predictive Maintenance*. In the context of the latter, the degree of deviation from an expected value represents the urgency to maintain a system. In this work, we focus on the detection of anomalies in temporal data. In general, outliers can be seen as *changes*, *sequences*, or *temporal patterns* [12]. Furthermore, there exist various anomaly types (see Fig. 1, [9]). In this context, the most common techniques that are used for an outlier detection constitute *classification* and *clustering*. Moreover, the field of outlier detection is related to *forecasting*, as deviations from expected values might indicate an unexpected change in the behavior of a machine. Nowadays, industrial production generates data in various resolutions and formats. Usually, the obtained sensor values have a very high resolution. In this context, data is assigned by

a *computer-aided quality assurance* (CAQ) to a higher hierarchy level if it has a lower resolution and vice versa. Therefore, outliers can be detected and utilized coming from different hierarchy levels, while these levels, in turn, have their different requirements towards the used algorithms, e.g., in terms of data types, calculation speed, and dimensionality. In this work, we provide a short overview of outlier detection methods and their purpose. Furthermore, we suggest a data structure for outlier detection that is based on the following idea: Machines are often equipped with redundant sensors, e.g., to measure the temperature of the same machine at different places. However, sensors measuring the same information allow for the calculation of a *support value* for outliers. Hereby, an outlier is more valuable if it is also found in the supporting sensor at the same time. Based on this idea, the suggested data structure shall be able to represent the supporting as well as the hierarchy value for an outlier.

The remainder of this paper is structured as follows. In Section 2, we briefly illustrate the hierarchical structure. Section 3 presents the categories of outliers that can be found in the literature, while Section 4 sketches an algorithm which incorporates the hierarchy. Related work is discussed in Section 5. Finally, a summary and an outlook are provided in Section 6.

## 2 HIERARCHICAL STRUCTURE

The production layers used in this work (see Fig. 2) contain different types of data and therefore a framework is introduced that can handle several types of outlier detection approaches as well as can combine their advantages with respect to specific data types. The first introduced layer is denoted as *phase level* (1). The production process is usually split into several phases, e.g., *preparation*, *warm-up*, and *calibration*. In the proposed model, this layer provides the most detailed view on the production. It comprises multi-dimensional, high-resolution sensor values that deliver either time series data or discrete value sequences during the corresponding phase. Time series data corresponds to numeric data over time, while discrete sequences are made of labels. In the *job level* (2), a whole production process is displayed. A job may consist of several phases and it starts with a setup and ends with a computer-aided quality (CAQ) check. The setup and quality tests are not time series, but provide nevertheless



Figure 1: Outlier Types

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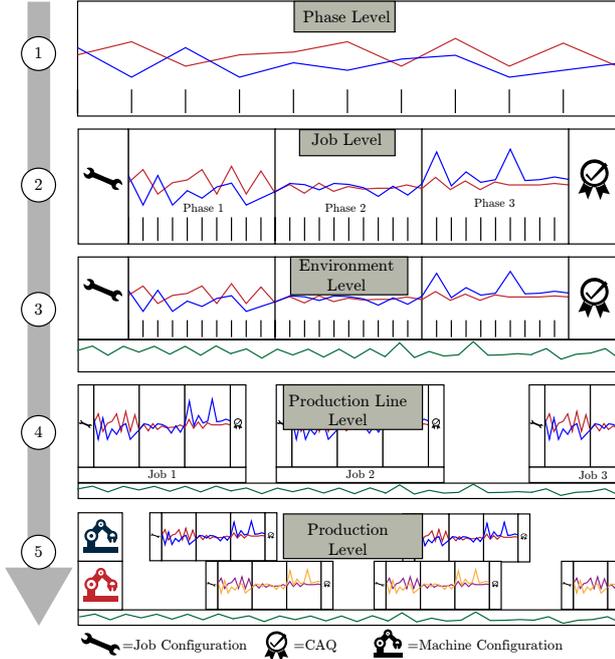


Figure 2: Outlier Types

high-dimensional data. During the setup, parameters are selected and the job is prepared. When considering the *environment-level* (3), a new time series is introduced, which does not correspond directly to the production process, but is measured in the same period. An example of such a time series would be the room temperature. If jobs over time are investigated (4), the high-dimensional setup provides also a time series. This layer, in turn, is denoted as *production line level*. Finally, the production level (5) includes data from different machines and represents therefore the most complex scenario. The aim of future work will be to combine outlier information from the different levels in a valuable manner.

### 3 CATEGORIZATION OF LITERATURE ON OUTLIERS

Due to the various scenarios in a production environment, different outlier detection algorithms should be kept in mind (see Table 1). In general, production levels with high resolution values should use sequences to represent the outliers as points since they are vulnerable to measurement errors. In contrast, for aggregated values, points can be used to represent outliers. In general, anomalies in time series can be extracted by a straightforward computation or by using overlapping fixed size windows, which, in turn, are aggregated. The first introduced technique in this context is called discriminative approach (DA). Thereby, a *similarity function* compares sequences and clusters, while the distance of a time series to the centroid of the nearest clusters denotes the anomaly score. In *unsupervised parametric approaches* (UPA), an anomaly is discovered if a sequence is unlikely to be generated from a specified summary model. In case of multidimensional data, an Online Analytical Processing (OLAP) cube can be analyzed, using an unsupervised approach (UOA) with each cell as a measure. When labeled training data is available, supervised

Table 1: Categorization of Literature on Outliers

Technique	Type	PTS	SSQ	TSS
Match Count Sequence Similarity [16]	DA		✓	
Longest Common Subsequence [2]	DA		✓	
Vibration Signature [28]	DA		✓	✓
Expectation-Maximization [30]	DA	✓	✓	✓
Phased $k$ -Means [36]	DA		✓	✓
Dynamic Clustering [37]	DA		✓	✓
Single-linkage clustering [32]	DA	✓	✓	✓
Principal Component Space [13]	DA		✓	✓
Support Vector Machine [6]	DA	✓	✓	✓
Self-Organizing Map [11]	DA	✓	✓	✓
Finite State Automata [25]	UPA	✓	✓	
Hidden Markov Models [7]	UPA	✓	✓	
Online Analytical Processing Cube [20]	UOA	✓	✓	
Rule Learning [18]	SA		✓	✓
Neural Networks [10]	SA	✓	✓	✓
Rule Based Classifier [19]	SA		✓	
Window Sequence [17]	NPD		✓	
Anomaly Dictionary [3]	NMD		✓	
Symbolic Representation [22]	OS		✓	✓
Autoregressive Model [15]	PM	✓	✓	
Histogram Representation [27]	ITM		✓	

DA=Discriminative Approach, UPA=Unsupervised Parametric Approach, UOA=Unsupervised Online Approach, SA=Supervised Approach, NPD=Normal Pattern Database, NMD=Negative and Mixed Pattern Database, OS=Outlier Subsequence, PM=Predictive Model, ITM= Information-Theoretic Model, PTS=Points, SSQ=Sequences, TSS=Time Series

approaches (SA) can be applied. *Window-based detection* is another type of outlier detection. Furthermore, outlier scores are calculated for overlapping windows with fixed length as parameters. This class of outlier detection suits well for detecting exact positions of anomalies. The *normal pattern database* (NPD), in turn, is a representative of a window-based approach. Regarding the latter, the frequencies of overlapping windows are stored in a database. If a new subsequence has many mismatches, it is considered as an anomaly. This procedure can be extended by not including only exact matches, but rather compute soft mismatch scores. In contrast to a NPD approach, the *negative and mixed pattern database* (NMD) is based on anomaly dictionaries. Here, test sequences are classified as anomalies if they match a sequence from the database. Next, to find *outlier subsequences* (OS), patterns are compared to their expected frequency in the database. The main problem is to preserve computational efficiency as the calculation of a match score and its permutations is very costly. *Prediction models* (PM) define the outlier score based on the delta value to the predicted value. In addition, prediction models are suitable for multi-variate time series. Another way to detect outliers is to compare a normal profile with new time points. This procedure is denoted as *profile similarity* (PS). Moreover, a *information-theoretic model* (ITM) detects outlier points by removing points from a sequel and measuring the improvement in a histogram-based representation. In this context, outlier points are denoted as *deviants*. Note that different type of outliers must be identified for each hierarchy in order to distinguish between outliers for finding *points* (pts), *sub-sequences* (ssq), or *time-series* (tss).

### 4 ALGORITHM

The work at hand proposes an algorithm (see Algorithm 1) for the utilization of outliers in a hierarchical production system. The result of the algorithm is represented by the triple *global score*, *outlierness*, and *support* (i.e., the data structure). First, the global score denotes in which of the five proposed levels the outlier was noticed. For example, if it was only recognized in the phase level, the global score value is low. Consequently, the higher a global score is, the more obvious was the outlier. Note that if outliers

are identified in a high production level, it is assumed that these outliers can be also identified in a lower level as well. Adversely, if no outlier can be found at a lower level, but in a higher level, a measurement error must be assumed. Second, the *outlierness* constitutes the significance of the outlier as computed by the actually used algorithm. Third, the *support* value can be increased if the outlier can be found in the same level for corresponding sensors, e.g., when the room temperature measurement supports another sensor measurement. In general, support values reduce the probability of finding a measurement error.

```

FindHierarchicalOutlier TS, LV
  inputs : startLevel(LV) and timeSeries(TS)
  output : <global score, outlierness, support>
  algorithm:=ChooseAlgorithm(startLevel);
  List<Sensors> correspondingSensors;
  List<Outlier> outlierList := CalculateOutlier(algorithm, startLevel,TS);
  foreach outlier ∈ outlierList do
    foreach sensor ∈ correspondingSensors do
      if sensor supports outlier then
        support++;
      end
    end
  end
  support/=Number of Corresponding Sensors;
  outlierness:=CalcOutlierness(algorithm);
  globalScore:= CalcGlobalScore(level++,true);
  CalcGlobalScore(level-,false);
CalcGlobalScore level, up
  algorithm =ChooseAlgorithm(level);
  CalculateOutlier(algorithm, level);
  if up then
    if Outlier Detected in Level then
      globalScore++; CalcGlobalScore(level++,true);
    end
  end
  else
    if No Outlier Detected in Level then
      Warning for Wrong Measurement;
    end
    else
      CalcGlobalScore(level-,false);
    end
  end

```

**Algorithm 1:** Outlier Hierarchical Algorithm

## 5 RELATED WORK

Outlier detection is also known as *anomaly detection*, *event detection*, *novelty detection*, *deviant discovery*, *change point detection*, *fault detection*, or *intrusion detection*. Based on an extensive literature study, Fig. 3 shows corresponding numbers of papers from each of these categories extracted from the search engine *Web of Science*. Note that each term was filtered with the word *time series* and afterwards limited to those items that are connected to the category *automation control systems*. In general, methods for outlier detection have been presented as general frameworks [39] as well as features for *process control systems* (PCS) [38]. Moreover, another challenge for outlier detection is related to the calculation speed. To tackle the latter, the authors of [4] used the MapReduce pattern to speed up the calculation for distance-based outliers. A further challenge in the field of outlier detection is the complexity of time series. Hereby, an approach for multivariate time series is introduced by [5]. To tackle the problem of large, noisy features, [31] used an outlier thresholding function for outlier selection, whose results are further on used as target feature. Another approach to deal with high dimensions constitutes the combination of outlier detection and dimension

reduction. In this context, [29] used the *principal component analysis* (PCA) and the *local outlier factor* (LOC) for a robust detection of noisy variables. In contrast, [26] extended the PCA with a factor leverage, which measures the influence of each data point of the PCA. A further way to reduce the dimension constitutes the use of *intrinsic dimensions* (ID). In [35], for example, the PCA is combined with a randomized approach for subspace recovery. Again, the dimension reduction method is combined with a local outlier score [41]. Due to the strong connection of outlier detection and the nearest neighbor method (knn), the effect of *hubness* needs to be considered (e.g., [34]). Note that hubness is denoted as the tendency of high-dimensional data to contain points from other *knn* lists. To summarize, all presented approaches help to tackle complex and large production data.

Another important part of related work can be referred to *outlierness scores*. For the production scenario used in this paper, flexible and adaptive outlier scores are needed, which can be expressed by the degree of outlierness. These scores allow for a ranking of outliers, which cannot be done using a binary outlier score, as the latter reveals only a decision for true/false decisions. In [14], for example, an interval-based approach is presented, in which the outlierness score is defined as the resulting distance after the clustering process. Hereby, it is possible to define a pattern as the ground truth prototype and all outlierness scores are relative to this selected pattern. A similar definition of outlierness score is presented by [23], in which it is denoted as the distance between a normal and the outlier class. The distance, in turn, is measured by a *Support Vector Machine*. Next, [21] enriches the outlierness score by including different context levels. For the levels *local*, *global*, and *ensemble*, an expected behavior is modeled and the outlierness refers to the difference between the expected and the measured value. Another approach uses the impact of outliers on the clustering objective, where the sensitivity denotes the worst-case impact of a point of the clustering solution [24]. Moreover, outlierness scores can be combined to outlier vectors, as, for example, pursued by [8]. This is especially helpful in the context of online outlier detection. Another way of expressing the degree of outlierness constitutes the evaluation of all distances to elements in the neighbor and by the use of the percentage of distances higher than the mean distance [33]. This concept is designed to work for dependent elements, as they can be found in graphs. The last presented outlierness approach [1] uses the imbalance between densities of all objects. Finally, sensors can be simulated using software, which is denoted as *soft sensor modeling*. A fusion of outlier detection and soft sensor modeling, for example, is presented by [40].

In the light of the presented approach, to the best of our knowledge, none of the evaluated related works deal with outlier detection in different hierarchy levels in an industrial production setting as we do.

## 6 SUMMARY AND OUTLOOK

We proposed a novel algorithm that includes three characteristics of outliers in a production environment, namely the global score, the outlierness, and the support. These values are calculated using different algorithms, whereby the algorithm should be selected with respect to the resolution best fitting to a production layer. This representation of outliers helps then to represent the importance of an outlier and classify the outliers by several criteria for a more transparent production. The review of various outlier methods has shown possible algorithm candidates that can

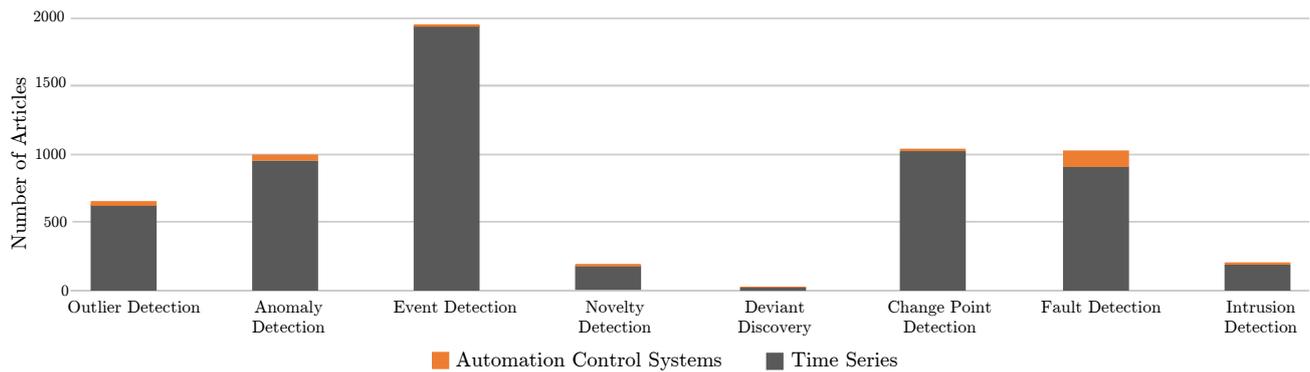


Figure 3: Research Fields of Outlier Detection

be used for the corresponding layers. Some of these algorithms fit better on time series, some of them on sequences, while others on outlier points. In future work, the approach will be evaluated based on real-life data of a company that produces machines in an industrial large-scale production setting.

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